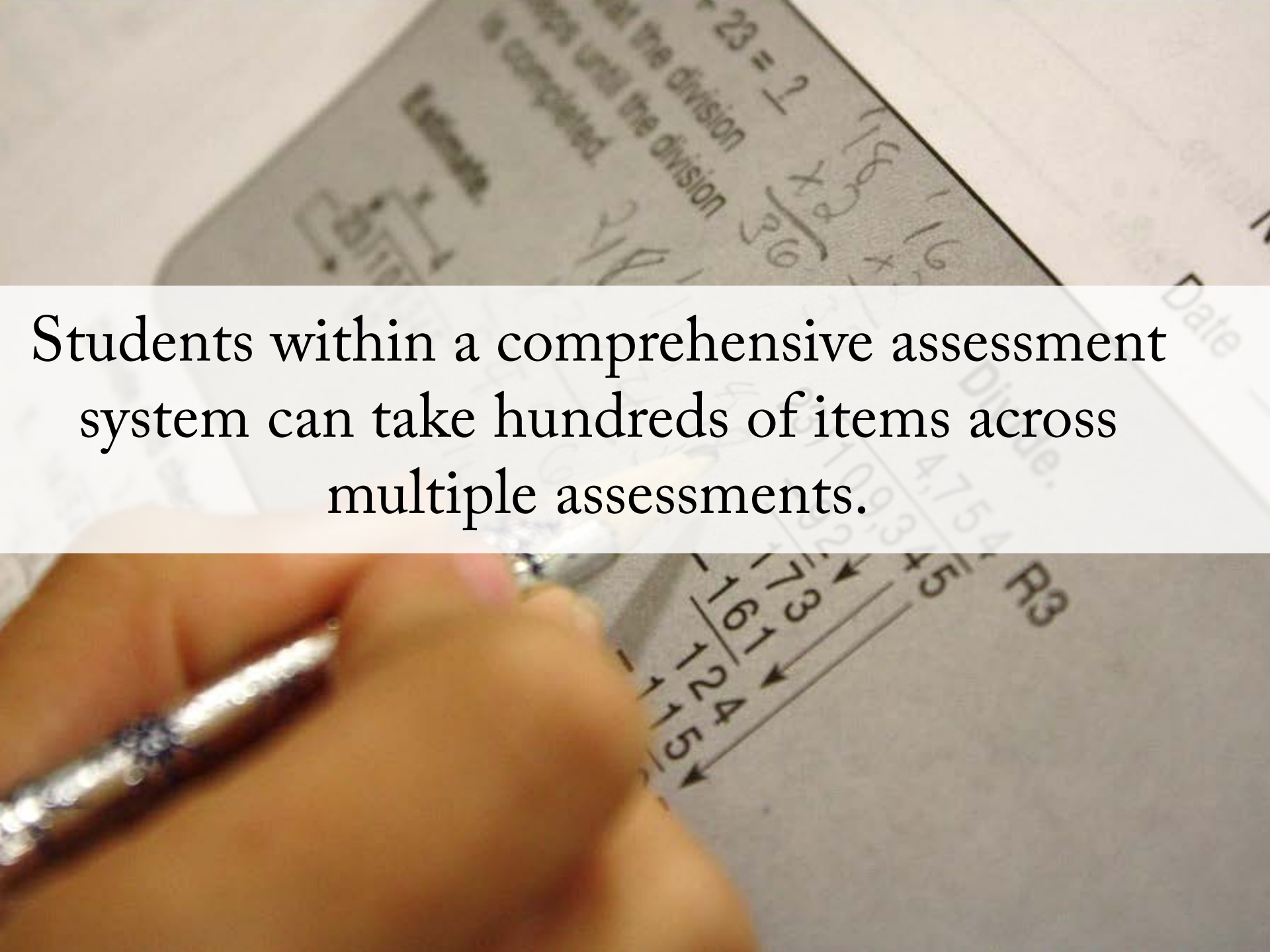


Synthesizing Evidence in a Comprehensive Assessment System

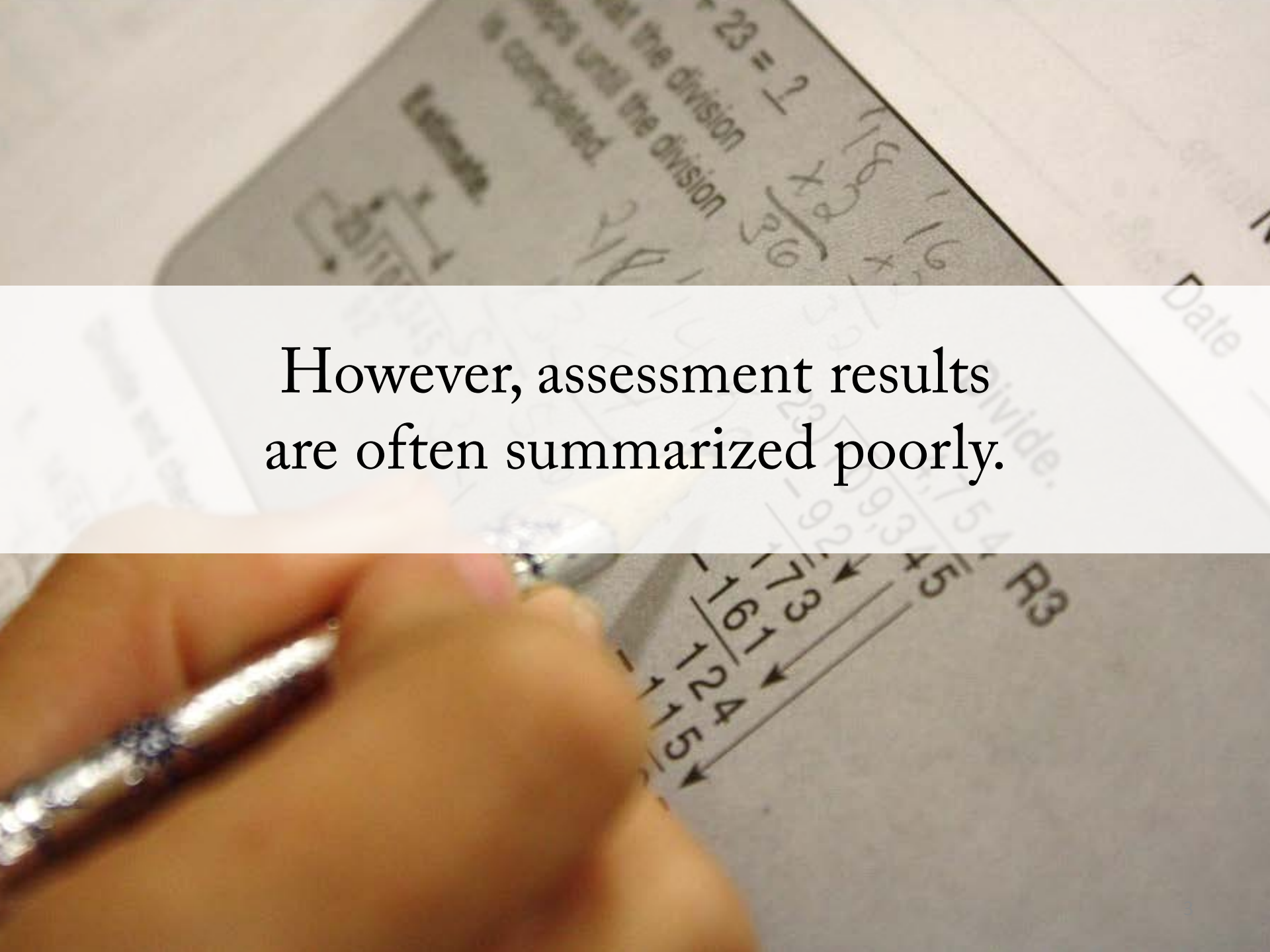
Nathan Dadey & Brian Gong
Center for Assessment

Reidy Interactive Lecture Series
September 17th, 2015





Students within a comprehensive assessment system can take hundreds of items across multiple assessments.

A hand holding a silver pen is positioned over a notebook page. The page contains several math problems, including a long division problem with arrows indicating steps and a multiplication problem. The text 'However, assessment results are often summarized poorly.' is overlaid on the page in a black serif font.

However, assessment results
are often summarized poorly.

The Goal: find a way to combine information
across multiple assessments

The Goal: find a way to combine information
across multiple assessments
for *all* assessment given *in* an academic year.

The Goal: find a way to combine information
across multiple assessments
for *all* assessment given *in* an academic year.

■
using a

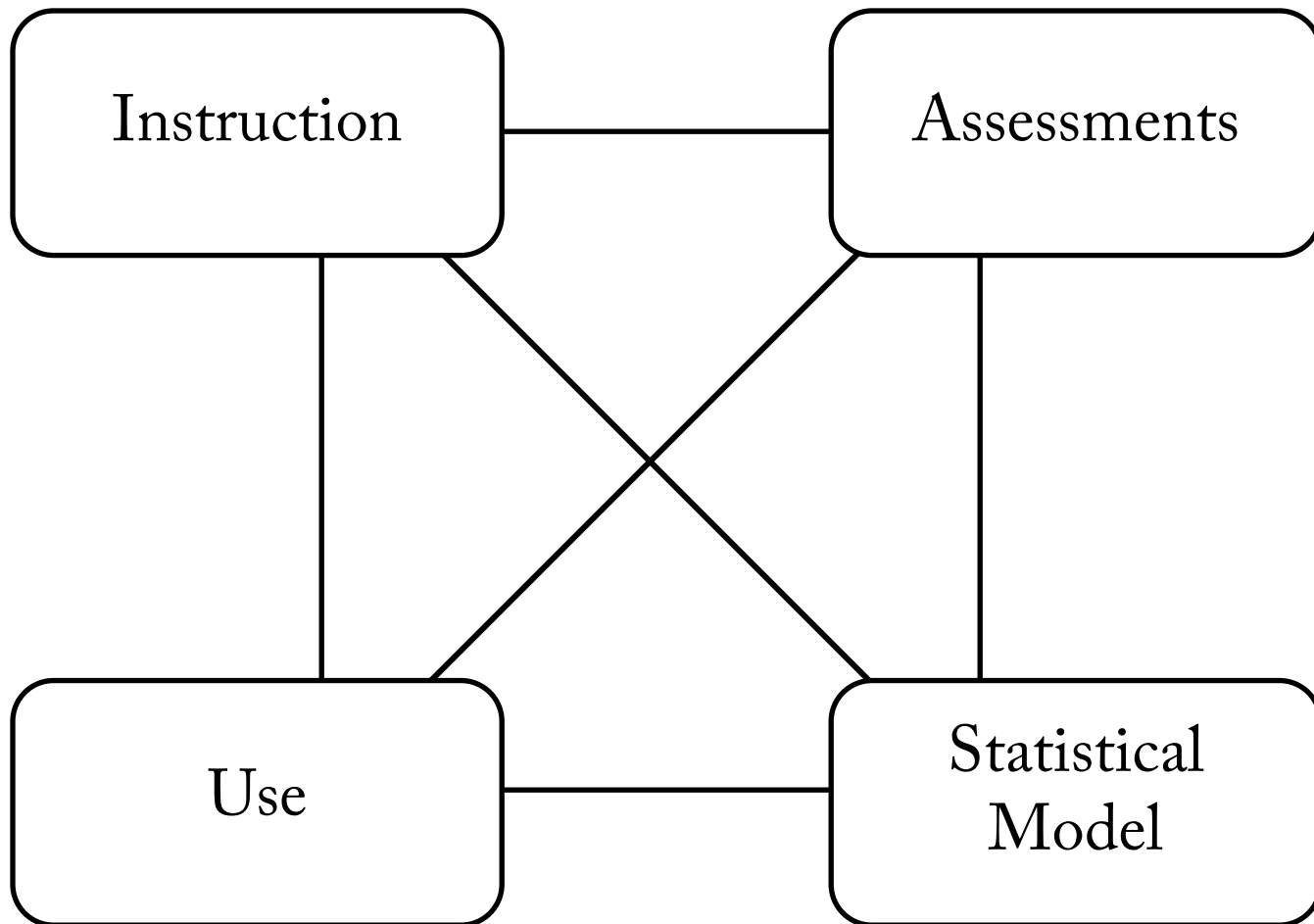


Statistical
Model

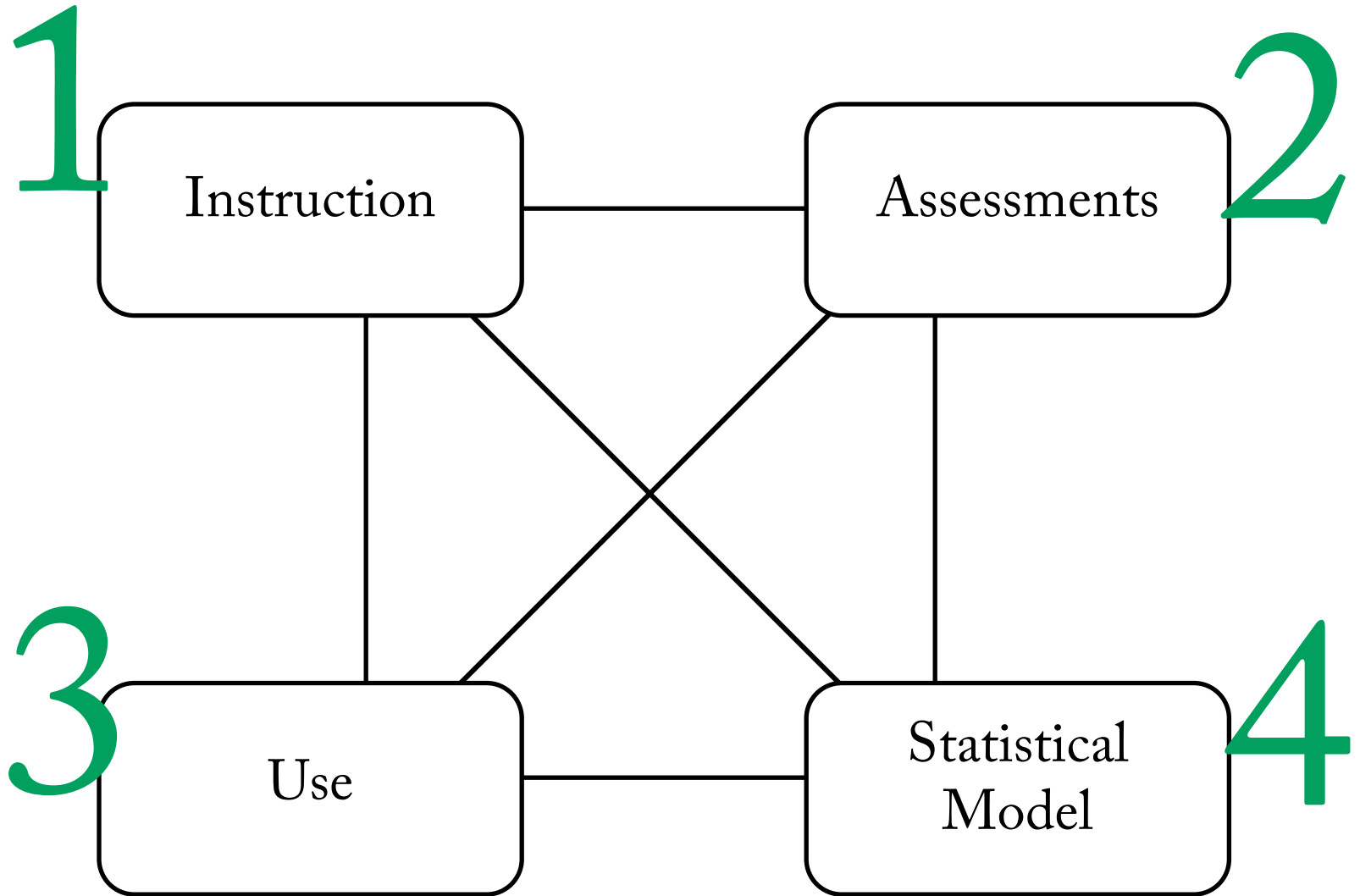
However, the results of such a model can't be understood in isolation.

Statistical
Model

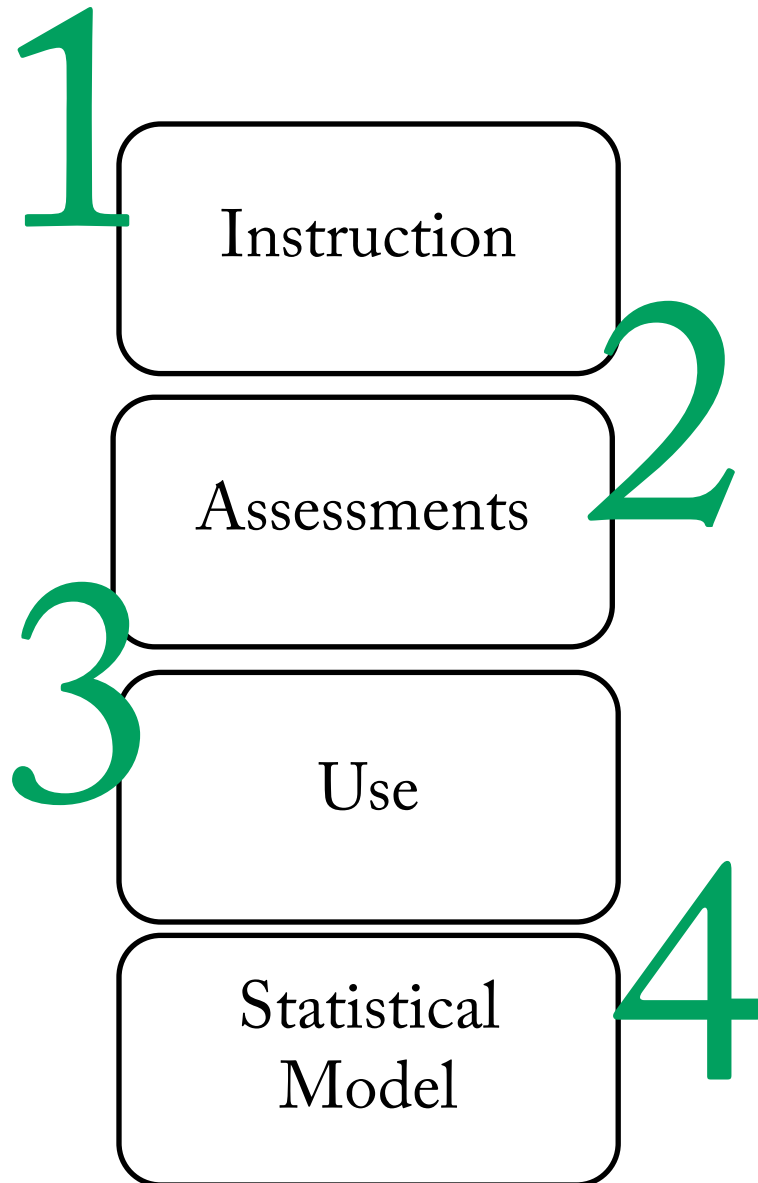
Interpretive Framework



Presentation Structure



Presentation Structure

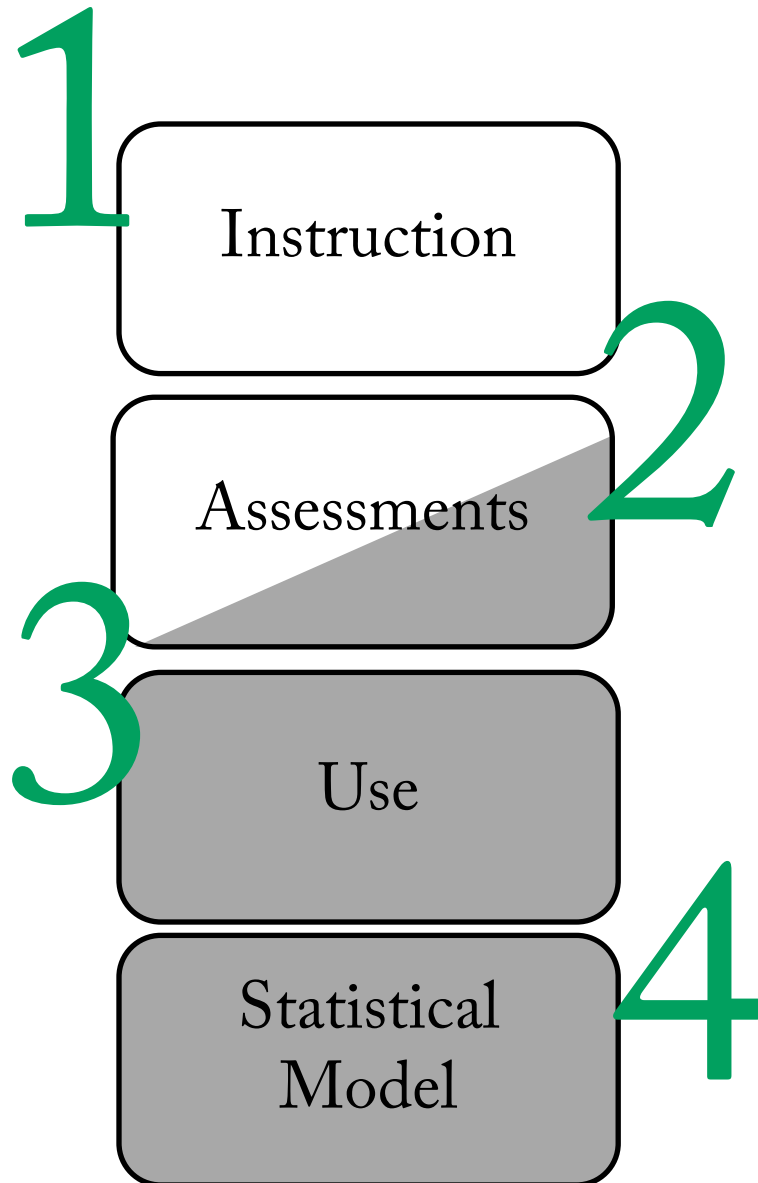


We examine these elements generally,

&

in terms of a specific hypothetical example.

Presentation Structure



We examine these elements generally,

&

in terms of a specific hypothetical example.


1 Instruction

Instruction

Scope & sequence of instruction, as captured by the ordering the Common Core State Standards.

Instruction

Scope & sequence of instruction, as captured by the ordering the Common Core State Standards.

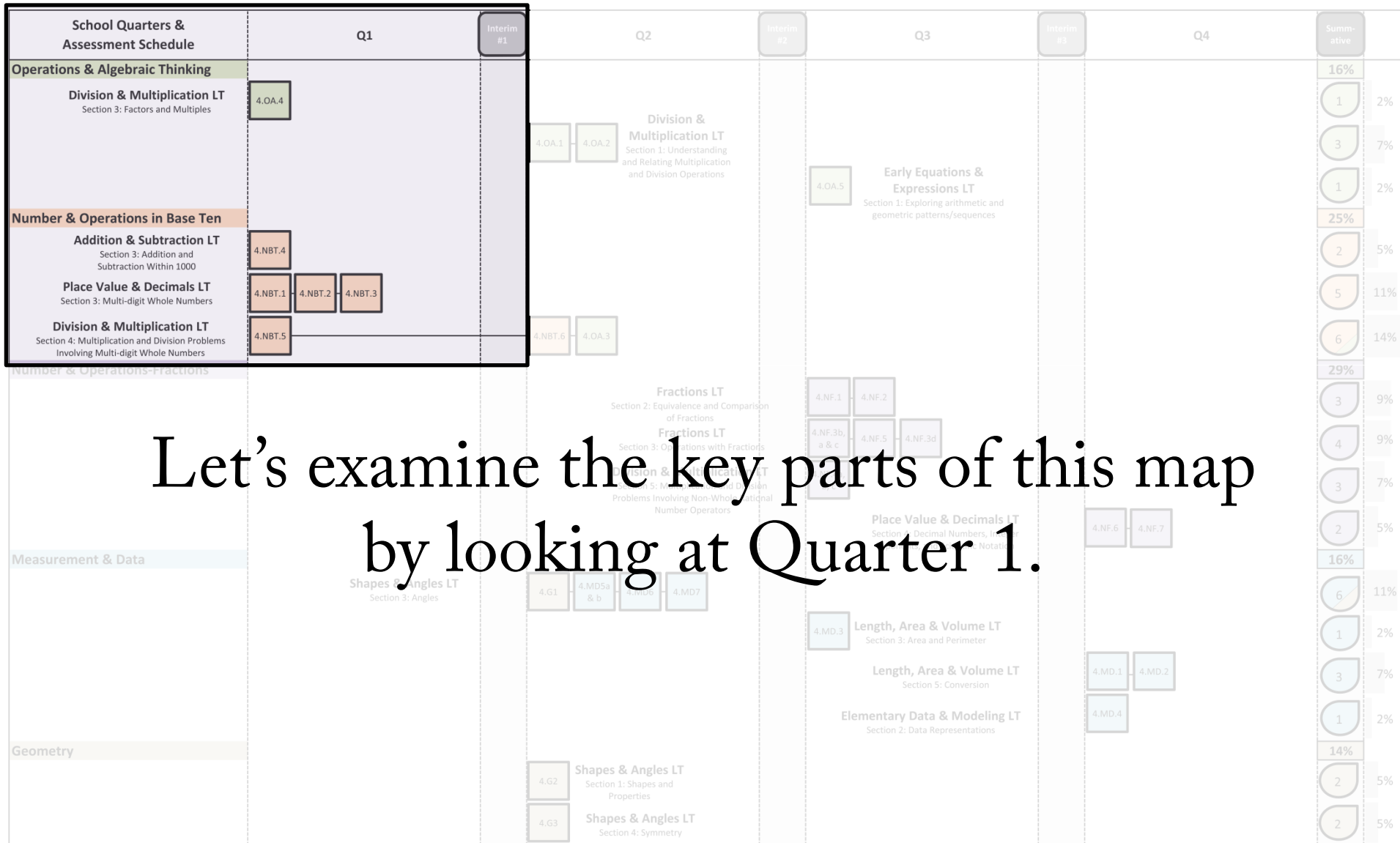


We show this as a Curriculum Map.

Curriculum Map

School Quarters & Assessment Schedule	Q1	Interim #1	Q2	Interim #2	Q3	Interim #3	Q4	Summative
Operations & Algebraic Thinking								16%
Division & Multiplication LT Section 3: Factors and Multiples	4.OA.4		4.OA.1 4.OA.2		4.OA.5			1 2% 3 7%
			Division & Multiplication LT Section 1: Understanding and Relating Multiplication and Division Operations		Early Equations & Expressions LT Section 1: Exploring arithmetic and geometric patterns/sequences			1 2%
Number & Operations in Base Ten								25%
Addition & Subtraction LT Section 3: Addition and Subtraction Within 1000	4.NBT.4							2 5%
Place Value & Decimals LT Section 3: Multi-digit Whole Numbers	4.NBT.1 4.NBT.2 4.NBT.3							5 11%
Division & Multiplication LT Section 4: Multiplication and Division Problems Involving Multi-digit Whole Numbers	4.NBT.5		4.NBT.6 4.OA.3					6 14%
Number & Operations-Fractions								29%
			Fractions LT Section 2: Equivalence and Comparison of Fractions		4.NF.1 4.NF.2			3 9%
			Fractions LT Section 3: Operations with Fractions		4.NF.3b, a & c 4.NF.5 4.NF.3d			4 9%
			Division & Multiplication LT Section 5: Multiplication and Division Problems Involving Non-Whole Rational Number Operators		4.NF.4a, b, c			3 7%
					Place Value & Decimals LT Section 4: Decimal Numbers, Integer Exponents, and Scientific Notation		4.NF.6 4.NF.7	2 5%
Measurement & Data								16%
	Shapes & Angles LT Section 3: Angles		4.G1 4.MD5a & b 4.MD6 4.MD7		4.MD.3			6 11%
					Length, Area & Volume LT Section 3: Area and Perimeter			1 2%
					Length, Area & Volume LT Section 5: Conversion		4.MD.1 4.MD.2	3 7%
					Elementary Data & Modeling LT Section 2: Data Representations		4.MD.4	1 2%
Geometry								14%
			4.G2					2 5%
			4.G3					2 5%

Curriculum Map



Let's examine the key parts of this map by looking at Quarter 1.

School Quarters & Assessment Schedule

Q1

Interim #1

Operations & Algebraic Thinking

Division & Multiplication LT
Section 3: Factors and Multiples

4.OA.4

Number & Operations in Base Ten

Addition & Subtraction LT
Section 3: Addition and Subtraction Within 1000

4.NBT.4

Place Value & Decimals LT
Section 3: Multi-digit Whole Numbers

4.NBT.1

4.NBT.2

4.NBT.3

Division & Multiplication LT
Section 4: Multiplication and Division Problems Involving Multi-digit Whole Numbers

4.NBT.5

Quarter & Assessment Administration

School Quarters & Assessment Schedule

Q1

Interim #1

Operations & Algebraic Thinking

Division & Multiplication LT
Section 3: Factors and Multiples

4.OA.4

Number & Operations in Base Ten

Addition & Subtraction LT
Section 3: Addition and Subtraction Within 1000

4.NBT.4

Place Value & Decimals LT
Section 3: Multi-digit Whole Numbers

4.NBT.1

4.NBT.2

4.NBT.3

Division & Multiplication LT
Section 4: Multiplication and Division Problems Involving Multi-digit Whole Numbers

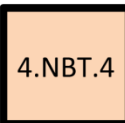
4.NBT.5

Each box is a 4th Grade CCSS.

Number & Operations in Base Ten

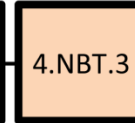
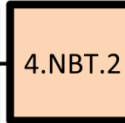
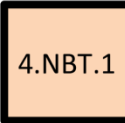
Addition & Subtraction LT

Section 3: Addition and
Subtraction Within 1000



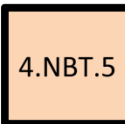
Place Value & Decimals LT

Section 3: Multi-digit Whole Numbers



Division & Multiplication LT

Section 4: Multiplication and Division Problems
Involving Multi-digit Whole Numbers



E.g.,

4.NBT.1

is Numbers & Operations in Base Ten,
Standard 1.

Number & Operations in Base Ten

Addition & Subtraction LT

Section 3: Addition and
Subtraction Within 1000

4.NBT.4

Place Value & Decimals LT

Section 3: Multi-digit Whole Numbers

4.NBT.1

4.NBT.2

4.NBT.3

Division & Multiplication LT

Section 4: Multiplication and Division Problems
Involving Multi-digit Whole Numbers

4.NBT.5

Each row is a section of a Learning Trajectory (LT). These LT sections are Drawn from Confrey et al.'s mapping of the CCSS.

Number & Operations in Base Ten

Addition & Subtraction LT

Section 3: Addition and Subtraction Within 1000

4.NBT.4

Place Value & Decimals LT

Section 3: Multi-digit Whole Numbers

4.NBT.1

4.NBT.2

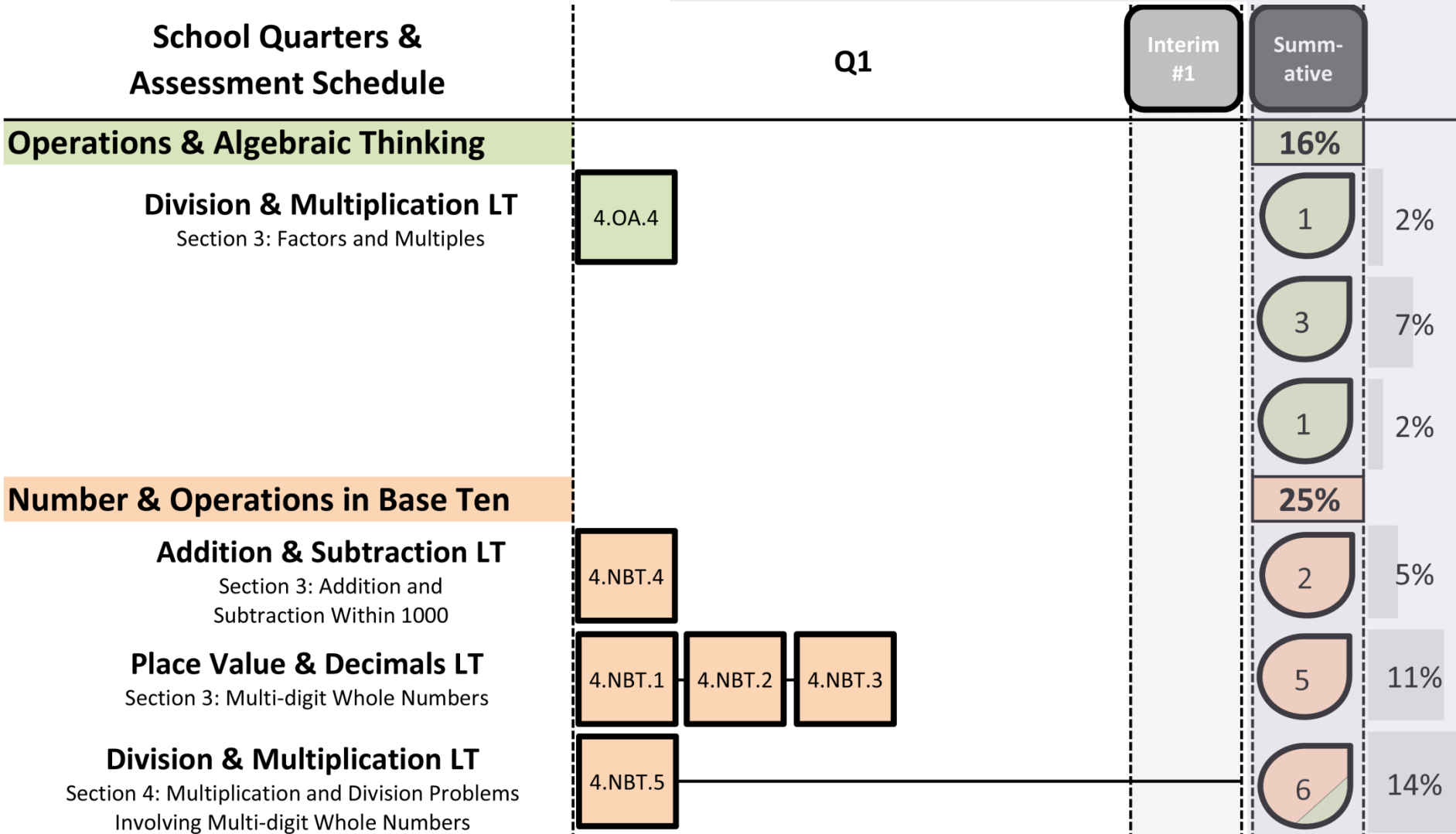
4.NBT.3

Division & Multiplication LT

Section 4: Multiplication and Division Problems Involving Multi-digit Whole Numbers

4.NBT.5

Summative Assessment



The first row shows the number of items per LT section.



Number & Operations in Base Ten

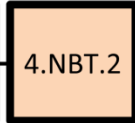
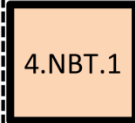
Addition & Subtraction LT

Section 3: Addition and Subtraction Within 1000



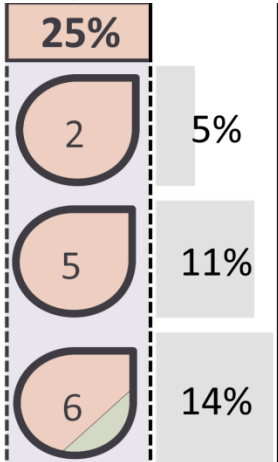
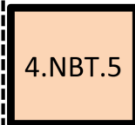
Place Value & Decimals LT

Section 3: Multi-digit Whole Numbers



Division & Multiplication LT

Section 4: Multiplication and Division Problems Involving Multi-digit Whole Numbers



The second row shows the percent of items per LT section.

Number & Operations in Base Ten

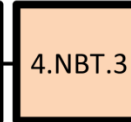
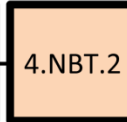
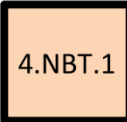
Addition & Subtraction LT

Section 3: Addition and Subtraction Within 1000



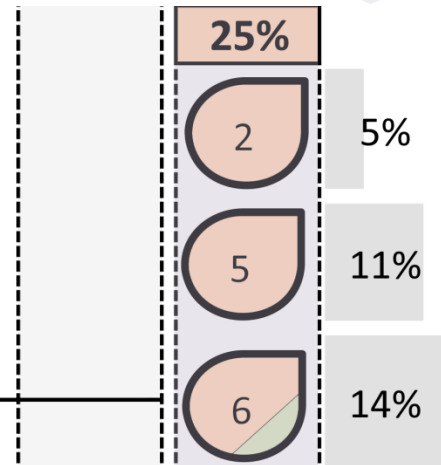
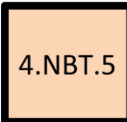
Place Value & Decimals LT

Section 3: Multi-digit Whole Numbers



Division & Multiplication LT

Section 4: Multiplication and Division Problems Involving Multi-digit Whole Numbers



Curriculum Map

School Quarters & Assessment Schedule	Q1	Interim #1	Q2	Interim #2	Q3	Interim #3	Q4	Summative
Operations & Algebraic Thinking								16%
Division & Multiplication LT Section 3: Factors and Multiples	4.OA.4		4.OA.1 4.OA.2		4.OA.5			1 2%
			Division & Multiplication LT Section 1: Understanding and Relating Multiplication and Division Operations					3 7%
								1 2%
Number & Operations in Base Ten								25%
Addition & Subtraction LT Section 3: Addition and Subtraction Within 1000	4.NBT.4							2 5%
Place Value & Decimals LT Section 3: Multi-digit Whole Numbers	4.NBT.1 4.NBT.2 4.NBT.3							5 11%
Division & Multiplication LT Section 4: Multiplication and Division Problems Involving Multi-digit Whole Numbers	4.NBT.5		4.NBT.6 4.OA.3					6 14%
Number & Operations-Fractions								29%
			Fractions LT Section 2: Equivalence and Comparison of Fractions		4.NF.1 4.NF.2			3 9%
			Fractions LT Section 3: Operations with Fractions		4.NF.3b, a & c 4.NF.5 4.NF.3d			4 9%
			Division & Multiplication LT Section 5: Multiplication and Division Problems Involving Non-Whole Rational Number Operators		4.NF.4a, b, c			3 7%
								2 5%
Measurement & Data								16%
	Shapes & Angles LT Section 3: Angles		4.G1 4.MD5a & b 4.MD6 4.MD7		4.MD.3			6 11%
								1 2%
					Length, Area & Volume LT Section 3: Area and Perimeter			3 7%
					Length, Area & Volume LT Section 5: Conversion		4.MD.1 4.MD.2	1 2%
					Elementary Data & Modeling LT Section 2: Data Representations		4.MD.4	1 2%
Geometry								14%
			4.G2					2 5%
			4.G3					2 5%

2 Assessment

Assessment

The LT Sections on each assessment, the number of items per LT, the scores reported, & when the assessments are given.

Assessment

The LT Sections on each assessment, the number of items per LT, the scores reported, & when the assessments are given.

Assessment

The LT Sections on each assessment,
the number of items per LT



Issues of design that cut across
“types” of assessments.

The LT Sections on each assessment
can be selected based on

The
summative
assessment.

Instruction.

A Post/Pre
Design.

The LT Sections on each assessment
can be selected based on

The
summative
assessment.

Instruction,
for this
example.

A Post/Pre
Design.

The number of items per LT section can

Equal.

Unequal.

The number of items per LT section can

Equal.

Unequal,
with emphasis
based on

Summative
Assessment.

District
Judgment.

The number of items per LT section can

Equal.

Unequal,
with emphasis
based on

Summative
Assessment.

District
Judgment.

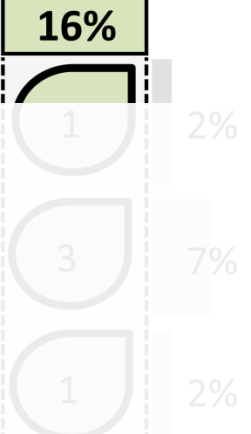
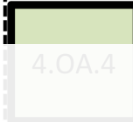
School Quarters & Assessment Schedule

Q1



Operations & Algebraic Thinking

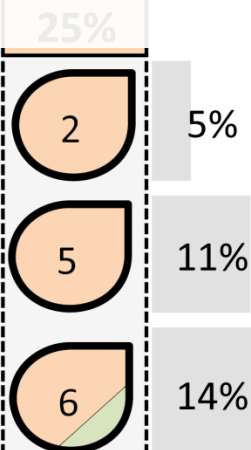
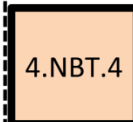
Division & Multiplication LT
Section 3: Factors and Multiples



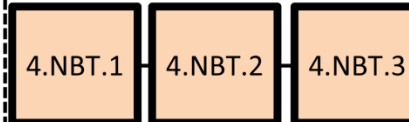
Let's look at what these choices look like for Interim #1.

Number & Operations in Base Ten

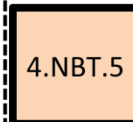
Addition & Subtraction LT
Section 3: Addition and Subtraction Within 1000



Place Value & Decimals LT
Section 3: Multi-digit Whole Numbers



Division & Multiplication LT
Section 4: Multiplication and Division Problems Involving Multi-digit Whole Numbers



School Quarters & Assessment Schedule

Q1



Operations & Algebraic Thinking

Division & Multiplication LT
Section 4: Factors and Multiples



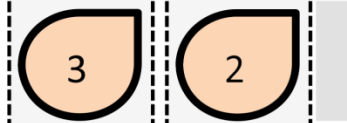
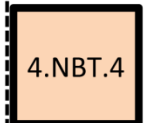
LT Sections: Instruction from Prior Quarter

Item Unequal, based on Summative

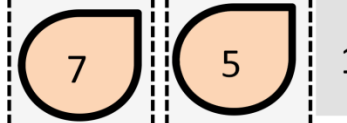
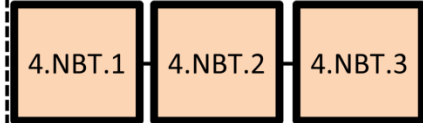
Distribution: Assessment

Number & Operations in Base Ten

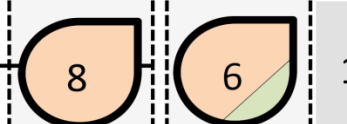
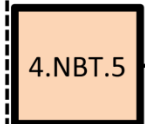
Addition & Subtraction LT
Section 3: Addition and Subtraction Within 1000



Place Value & Decimals LT
Section 3: Multi-digit Whole Numbers



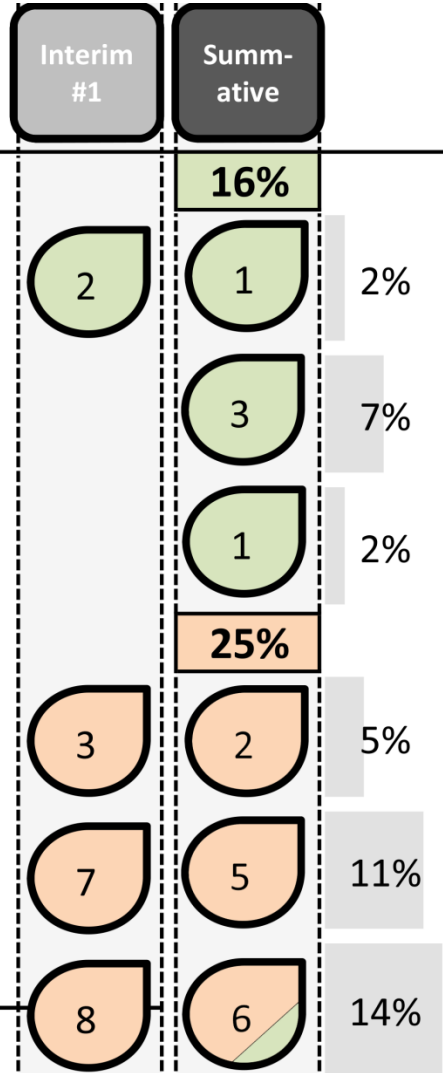
Division & Multiplication LT
Section 4: Multiplication and Division Problems Involving Multi-digit Whole Numbers



25%

School Quarters & Assessment Schedule

Q1



Operations & Algebraic Thinking

Division & Multiplication LT
Section 3: Factors and Multiples

4.OA.4

2

1

2%

3

7%

1

2%

Number & Operations in Base Ten

Addition & Subtraction LT
Section 3: Addition and Subtraction Within 1000

4.NBT.4

3

2

5%

Place Value & Decimals LT
Section 3: Multi-digit Whole Numbers

4.NBT.1

4.NBT.2

4.NBT.3

7

5

11%

Division & Multiplication LT
Section 4: Multiplication and Division Problems Involving Multi-digit Whole Numbers

4.NBT.5

8

6

14%

3

Use

Use

The purpose of the assessment system and the theory of action that supports it.

Purpose

Diagnostic

Predictive

Evaluative

Purpose

Diagnostic

Predictive

Evaluative

Purpose

Diagnostic

Prediction of
Student
Performance
on Summative
Assessment
based on

Interim
#1

&

Interim
#2


Evaluative

Purpose

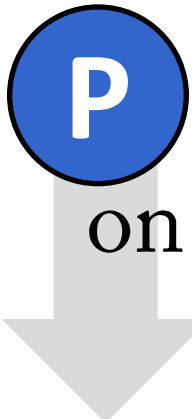
Diagnostic

P
=
I1
&
I2


Evaluative


What is  ?

P is a prediction of performance on the summative assessment.

 **P** is a prediction of performance
on the summative assessment,

based on a statistical model, e.g.,
linear regression,
Bayesian network, or
tree model.


Teachers use  to
inform their instructional decisions.

Teachers use  to
inform their instructional decisions.



Extra support within the classroom
Extra support outside the classroom
Extended support outside of the classroom
Intensive support outside of the classroom

see the work of Phil Daro.

Teachers use  to
inform their instructional decisions.



Extra support within the classroom
Extra support outside the classroom
Extended support outside of the classroom
Intensive support outside of the classroom

see the work of Phil Daro.

Theory of Action

Inputs

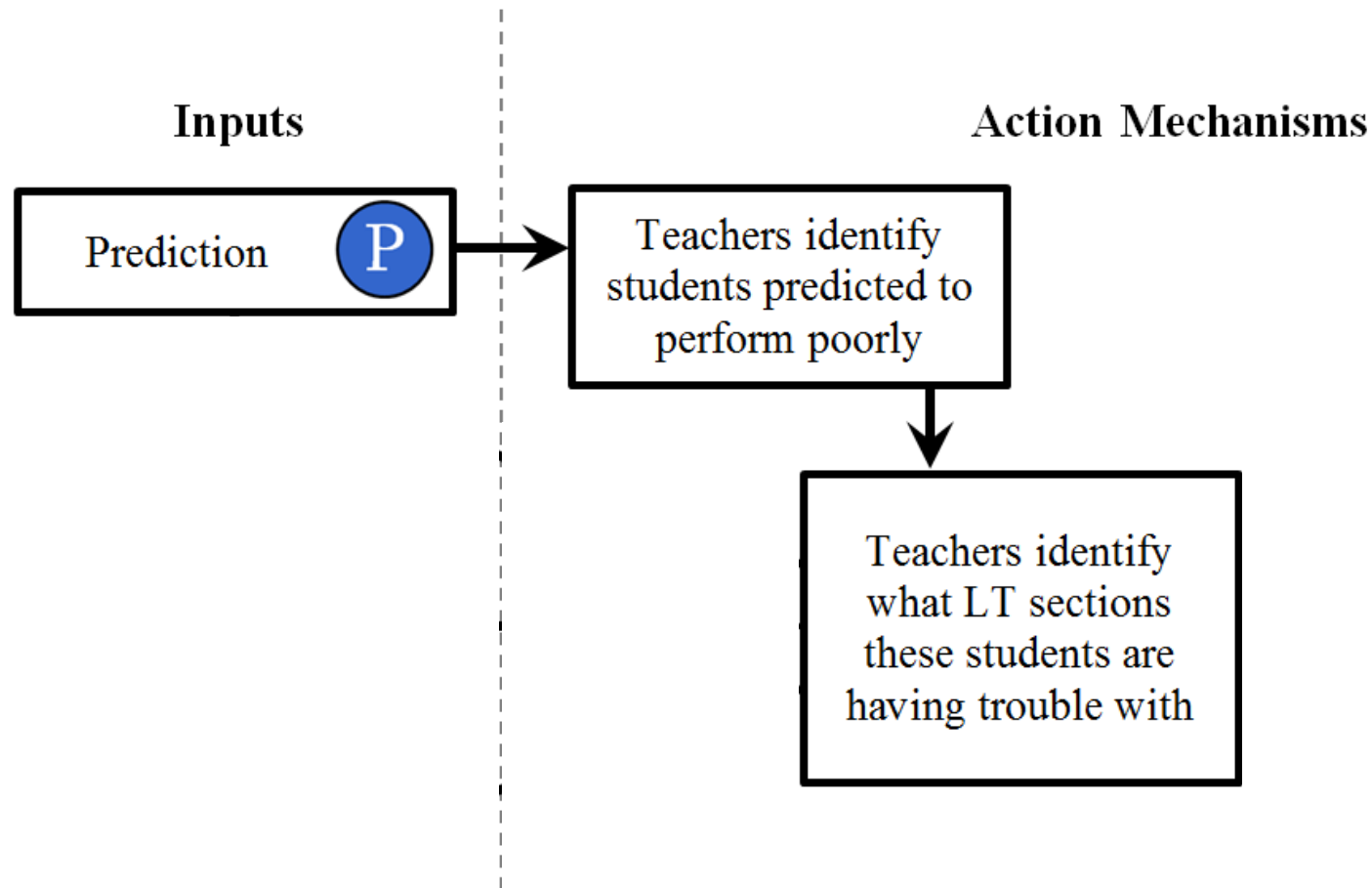
Prediction



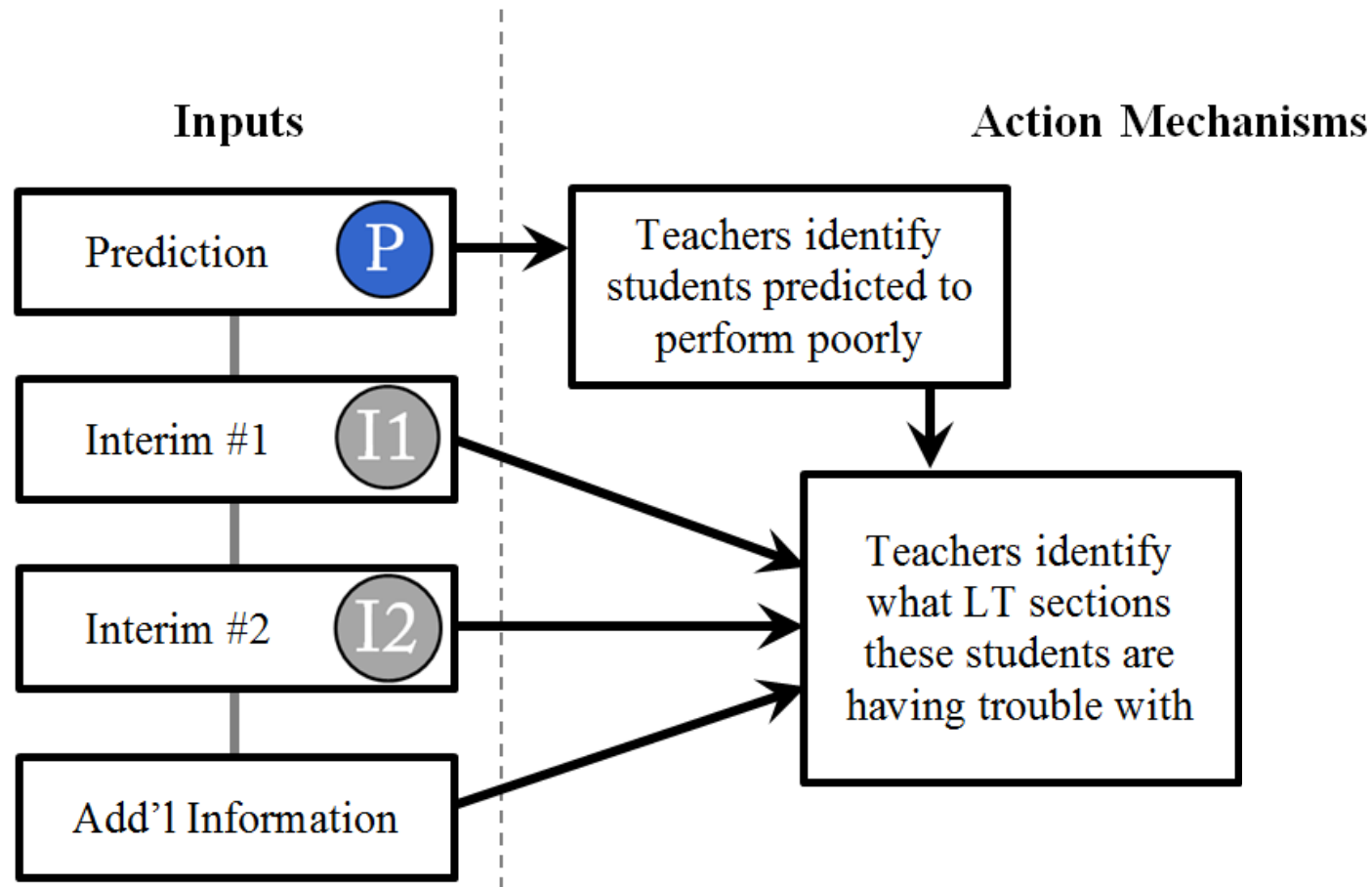
Action Mechanisms

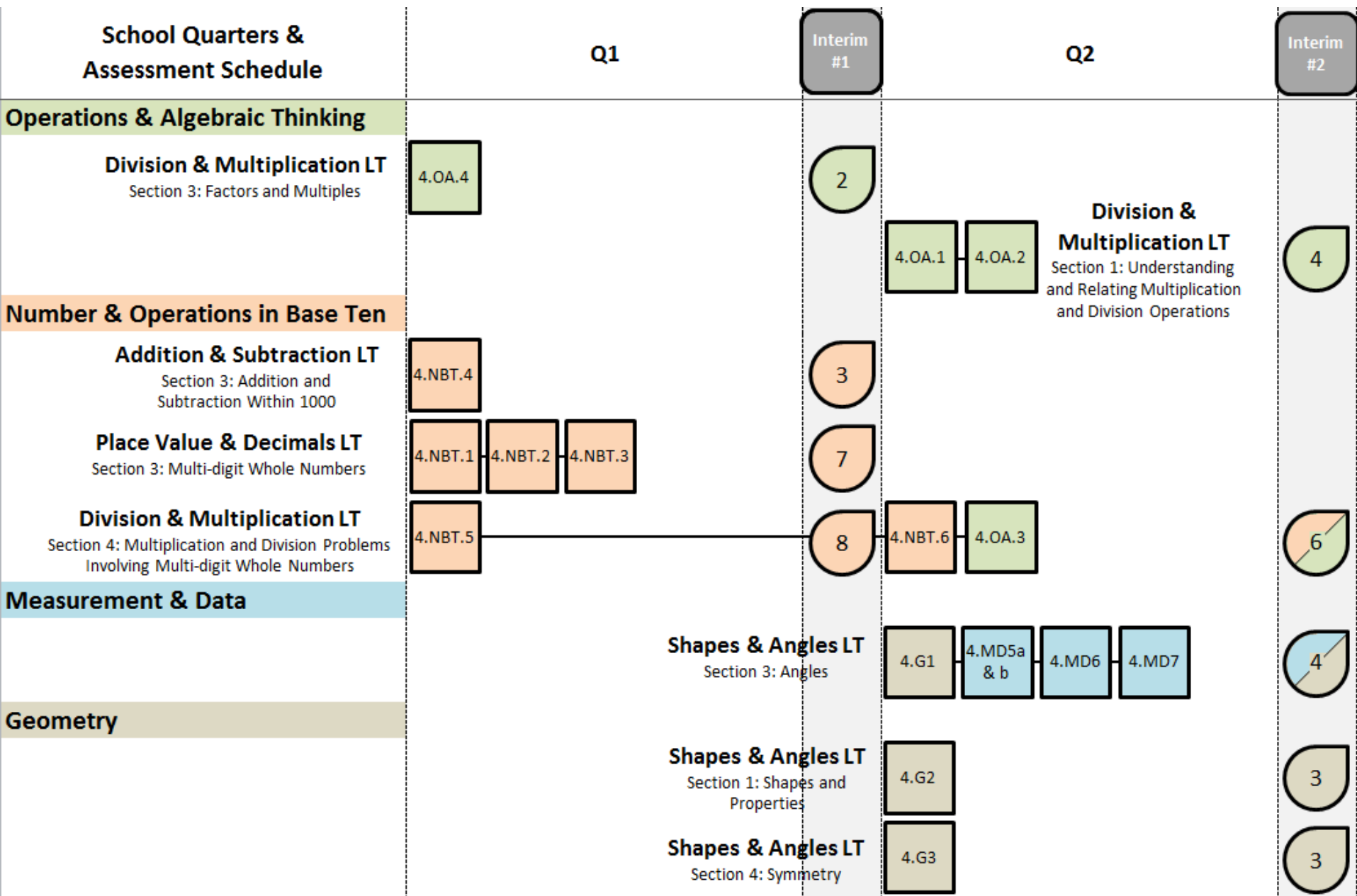
Teachers identify
students predicted to
perform poorly

Theory of Action



Theory of Action





School Quarters & Assessment Schedule

Q1

Interim #1

Q2

Interim #2

Operations & Algebraic Thinking

Division & Multiplication LT
Section 3: Factors and Multiples

4.OA.4

2

Division & Multiplication LT
Section 1: Understanding and Relating Multiplication and Division Operations

4.OA.1 4.OA.2

1

Teachers need to figure out what LT Sections students with low **P** are having trouble with.



Division & Multiplication LT
Section 4: Multiplication and Division Problems Involving Multi-digit Whole Numbers

4.NBT.5

8

4.NBT.6

4.OA.3

6

Measurement & Data

Shapes & Angles LT
Section 3: Angles

4.G1

4.MD5a & b

4.MD6

4.MD7

4

Geometry

Shapes & Angles LT
Section 1: Shapes and Properties

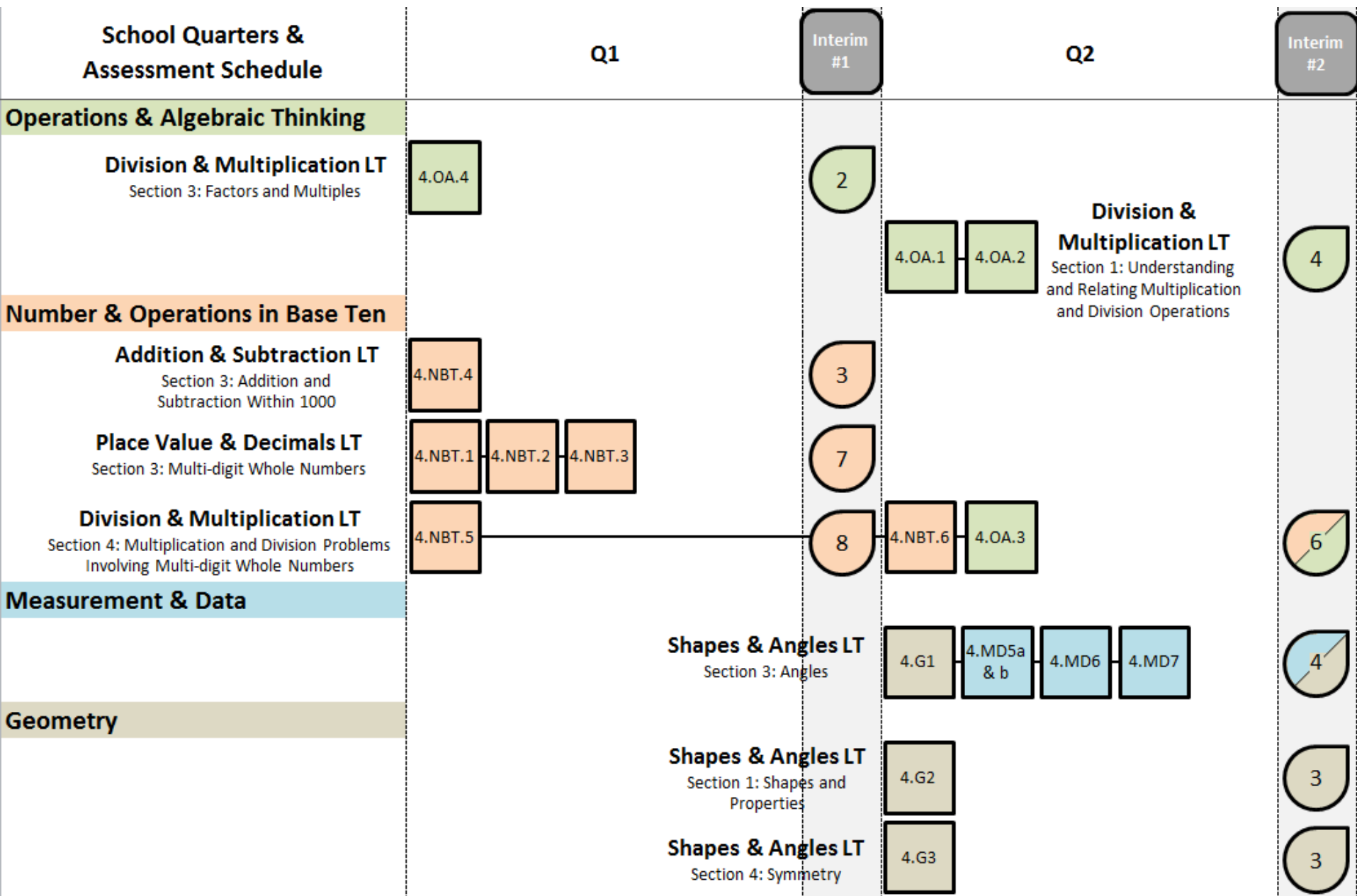
4.G2

3

Shapes & Angles LT
Section 4: Symmetry

4.G3

3



School Quarters & Assessment Schedule

Q1

Interim #1

Q2

Interim #2

Operations & Algebraic Thinking

Division & Multiplication LT
Section 3: Factors and Multiples

4.OA.4

2

4.OA.1

4.OA.2

Division & Multiplication LT
Section 1: Understanding and Relating Multiplication and Division Operations

4

Number & Operations in Base Ten

Addition & Subtraction LT
Section 3: Addition and Subtraction Within 1000

4.NBT.4

3

Place Value & Decimals LT
Section 3: Multi-digit Whole Numbers

4.NBT.1

4.NBT.2

4.NBT.3

7

Division & Multiplication LT
Section 4: Multiplication and Division Problems Involving Multi-digit Whole Numbers

4.NBT.5

8

4.NBT.6

4.OA.3

6

Measurement & Data

Shapes & Angles LT
Section 3: Angles

4.G1

4.MD5a & b

4.MD6

4.MD7

4

Geometry

Shapes & Angles LT
Section 1: Shapes and Properties

4.G2

3

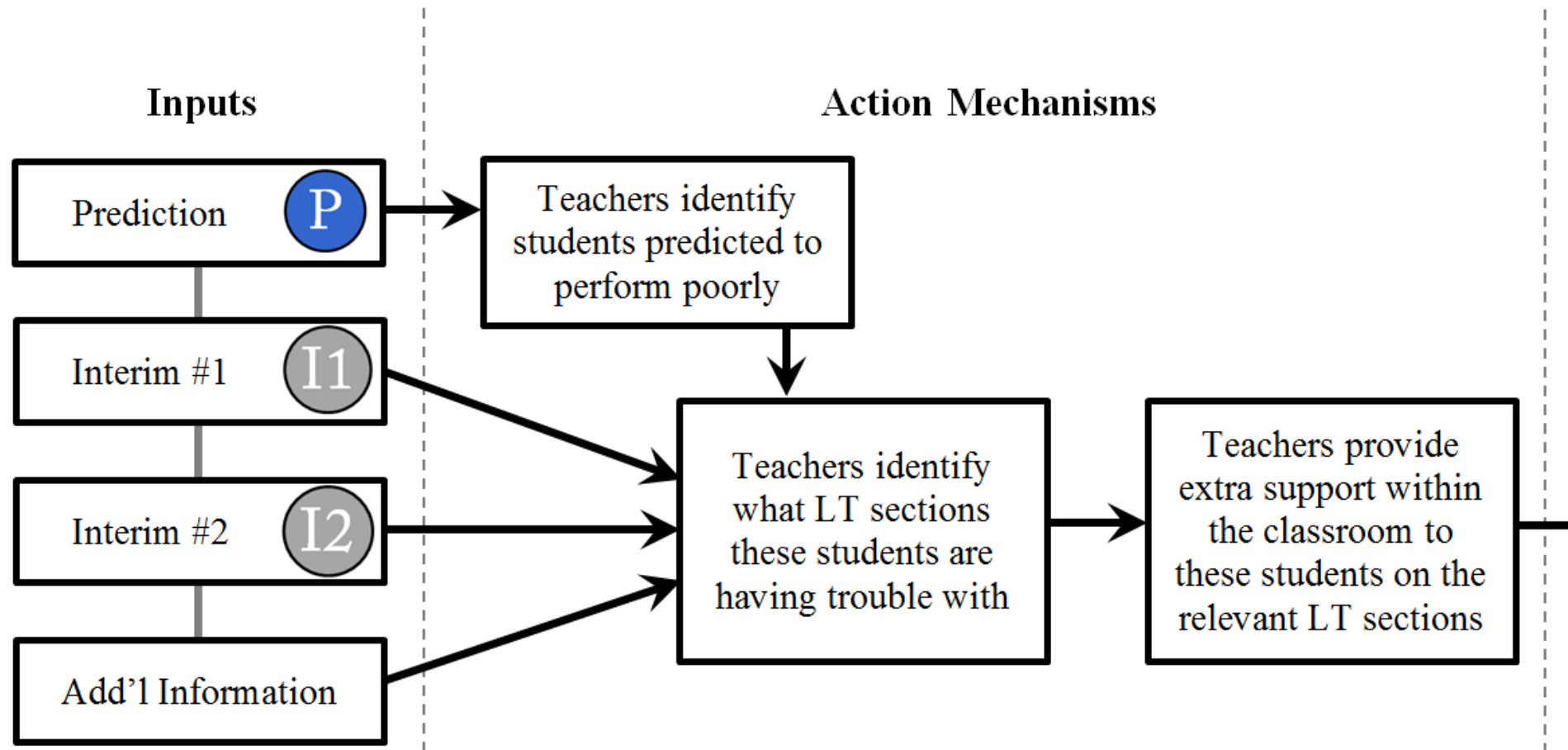
Shapes & Angles LT
Section 4: Symmetry

4.G3

3

Let's say it's the
Shapes & Angles LT, Section 3: Angles.

Theory of Action



School Quarters & Assessment Schedule

Q3

Interim #3

Operations & Algebraic Thinking

Early Equations & Expressions LT

Section 1: Exploring arithmetic and geometric patterns/sequences

4.OA.5

2

Number & Operations-Fractions

Fractions LT

Section 2: Equivalent Fractions and Operations with Fractions

Regular Instruction for Quarter 3.

Fractions LT

Section 3: Operations with Fractions

4.NF.1

4.NF.2

4.NF.3b, a & c

4.NF.5

4.NF.3d

5

6

Division & Multiplication LT

Section 5: Multiplication and Division Problems Involving Non-Whole Rational Number Operators

4.NF.4a, b, c

5

Measurement & Data

Length, Area & Volume LT

Section 3: Area and Perimeter

4.MD.3

2

School Quarters & Assessment Schedule

Q3

Interim #3

Operations & Algebraic Thinking

Early Equations & Expressions LT

Section 1: Exploring arithmetic and geometric patterns/sequences

4.OA.5

2

Number & Operations-Fractions

Fractions LT

Section 2: Equivalence and Comparison of Fractions

4.NF.1

4.NF.2

5

Fractions LT

Section 3: Operations with Fractions

4.NF.3b,
a & c

4.NF.5

4.NF.3d

6

Division & Multiplication LT

Section 5: Multiplication and Division Problems Involving Non-Whole Rational Number Operators

4.NF.4a,
b, c

5

Measurement & Data

Length, Area & Volume LT

Section 3: Area and Perimeter

4.MD.3

2

School Quarters & Assessment Schedule

Q3

Interim #3

Operations & Algebraic Thinking

Early Equations & Expressions LT

Section 1: Exploring arithmetic and geometric patterns/sequences

4.OA.5

2

Number & Operations-Fractions

Fractions LT

Instruction for students with low **P**.

Fractions LT

Section 3: Operations with Fractions

4.NF.1

4.NF.2

4.NF.3b, a & c

4.NF.5

4.NF.3d

5

6

Division & Multiplication LT

Section 5: Multiplication and Division Problems Involving Non-Whole Rational Number Operators

4.NF.4a, b, c

5

Measurement & Data

Length, Area & Volume LT

Section 3: Area and Perimeter

4.MD.3

2

Shapes & Angles LT

Section 3: Angles

4.G1

4.MD5a & b

4.MD6

4.MD7

School Quarters & Assessment Schedule

Q3

Interim #3

Operations & Algebraic Thinking

Early Equations & Expressions LT

Section 1: Exploring arithmetic and geometric patterns/sequences

4.OA.5

2

Number & Operations-Fractions

Fractions LT

Section 2: Equivalence and Comparison of Fractions

4.NF.1

4.NF.2

5

Fractions LT

Section 3: Operations with Fractions

4.NF.3b,
a & c

4.NF.5

4.NF.3d

6

Division & Multiplication LT

Section 5: Multiplication and Division Problems Involving Non-Whole Rational Number Operators

4.NF.4a,
b, c

5

Measurement & Data

Length, Area & Volume LT

Section 3: Area and Perimeter

4.MD.3

2

Shapes & Angles LT

Section 3: Angles

4.G1

4.MD5a
& b

4.MD6

4.MD7

School Quarters & Assessment Schedule

Q3

Interim #3

Operations & Algebraic Thinking

Early Equations & Expressions LT

Section 1: Exploring arithmetic and geometric patterns/sequences

4.OA.5

2

Number & Operations-Fractions

Fractions LT

Section 2: Equivalent Fractions and Operations on Fractions

4.NF.1

4.NF.2

5

Fractions LT

Section 3: Operations with Fractions and Mixed Numbers

4.NF.3

4.NF.4

6

Division & Multiplication LT

Section 5: Multiplication and Division Problems Involving Non-Whole Rational Number Operators

4.NF.4a, b, c

5

Measurement & Data

Length, Area & Volume LT

Section 3: Area and Perimeter

4.MD.3

2

Shapes & Angles LT

Section 3: Angles

4.G.1

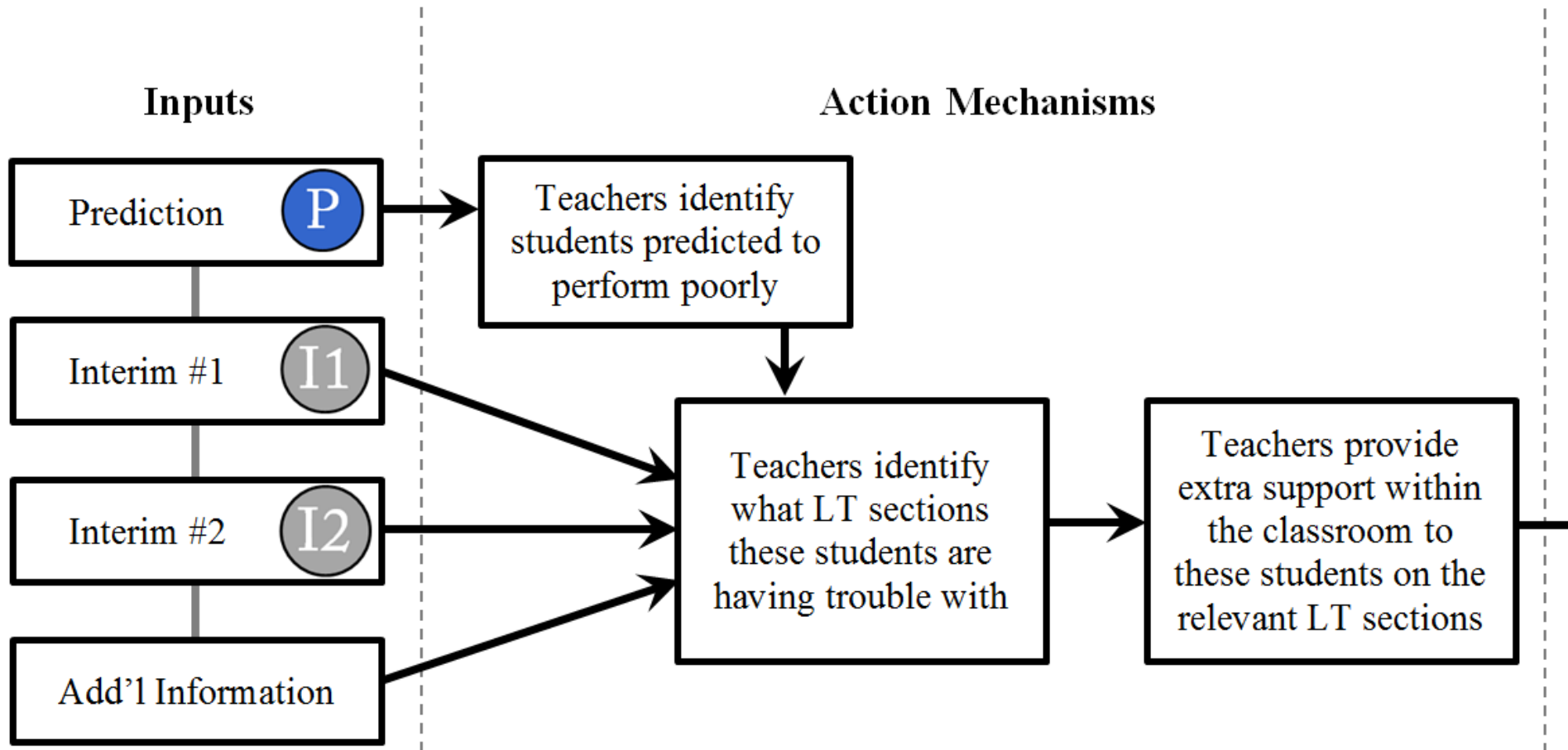
4.MD5a & b

4.MD6

4.MD7

These students must be taught all of the third quarter LT sections plus an extra LT section.

Theory of Action



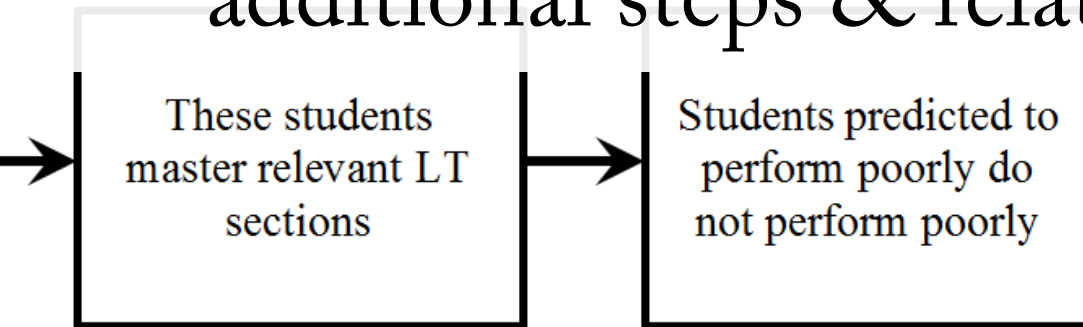
Theory of Action

Effects

Intermediate

Ultimate

Even if a teacher does these actions,
attaining the ultimate effect relies on
additional steps & related assumptions.

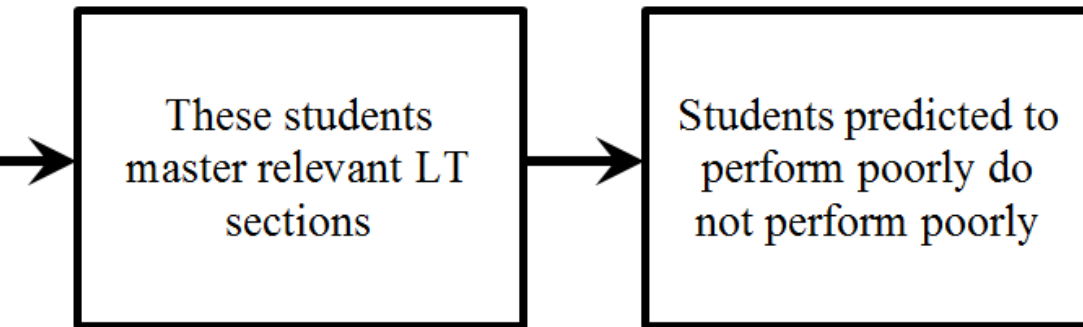


Theory of Action

Effects

Intermediate

Ultimate



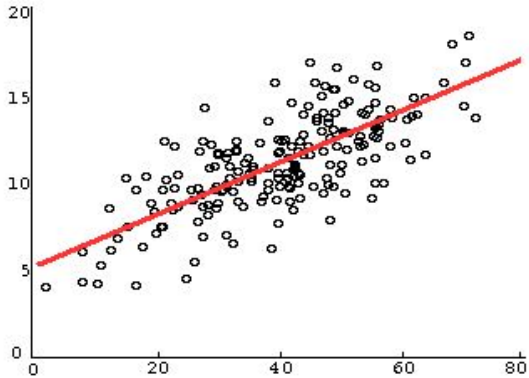
4

Statistical Model

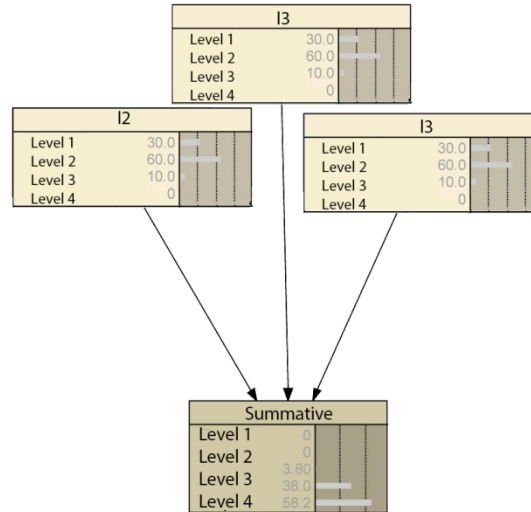
Statistical Model

The model used and their benefits.

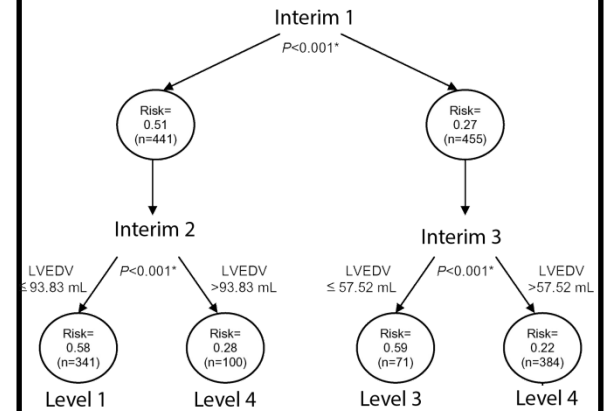
Some Possible Models



Regression



Bayesian Networks



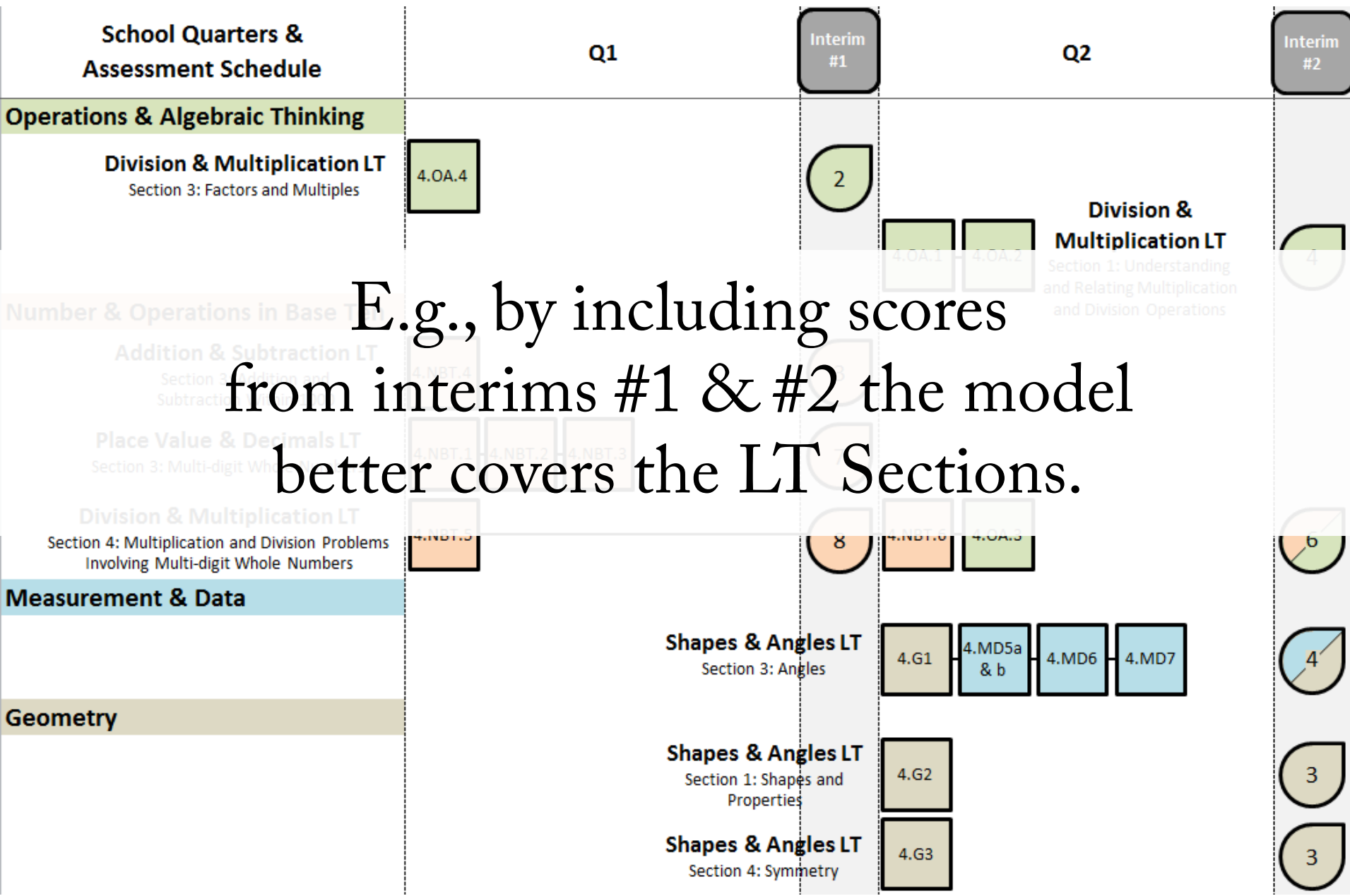
Tree Models

Despite their differences, these models
have many of the same benefits.

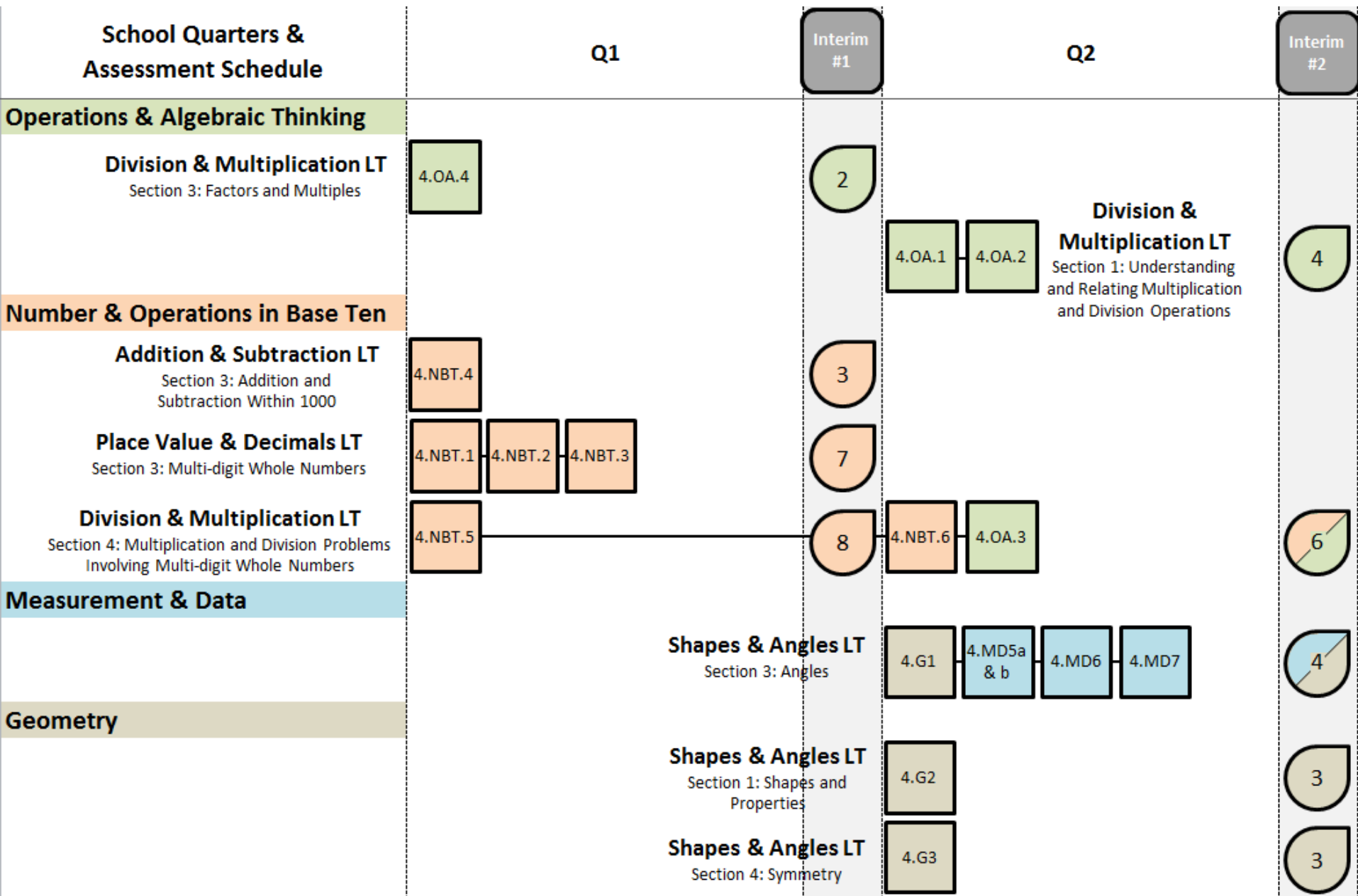
Despite their differences, these models
have many of the same benefits.



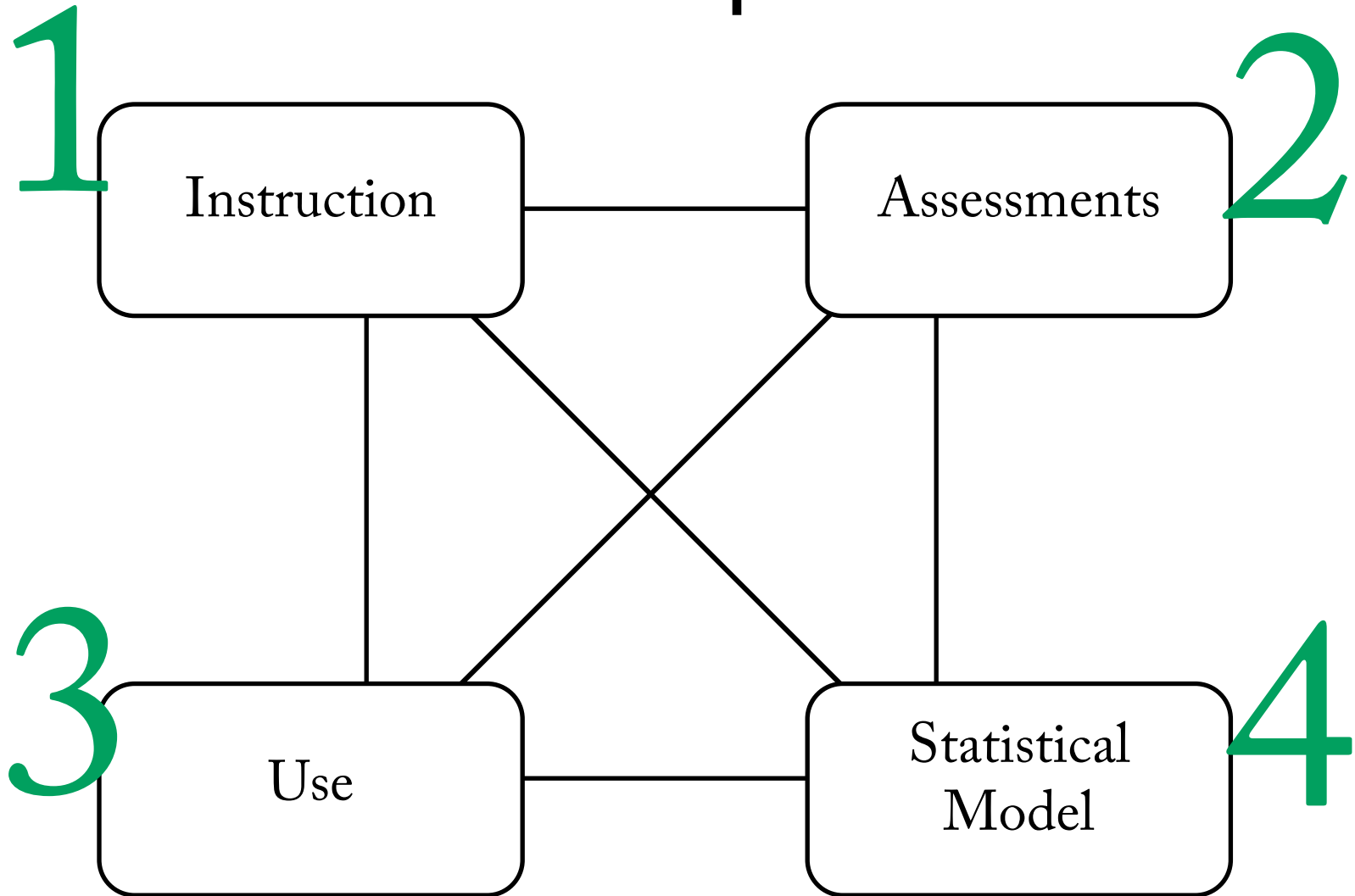
Better coverage of LT Sections
Parameterization Relationships between Assessments
Incorporate Additional Information
Increased Accuracy



E.g., by including scores from interims #1 & #2 the model better covers the LT Sections.



Recap



Modeling results from multiple assessments can add value, but interpretation depends on the other elements.

Modeling results from multiple assessments can add value, but interpretation depends on the other elements.

However,

the articulation of each element is valuable in its own right.

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